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**A STUDY OF COMPOSITE PLATES WITH HOLES/INCLUSIONS**

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## MODEL DESCRIPTION

Delamination characterization of a plate with a hole/inclusion is presented. A closed form solution is developed to obtain stresses on the boundary of hole/inclusion in the plate. Once the location with highest tangential stress is identified, FEM analysis of a laminate under tensile loading is considered. The models for the closed form and FEM are given in Figure 1 A & B. The examples are for  $[\pm 35/0/90]_s$  laminate of AS4/3501-6. Tensile, Biaxial and Shear loads are considered.

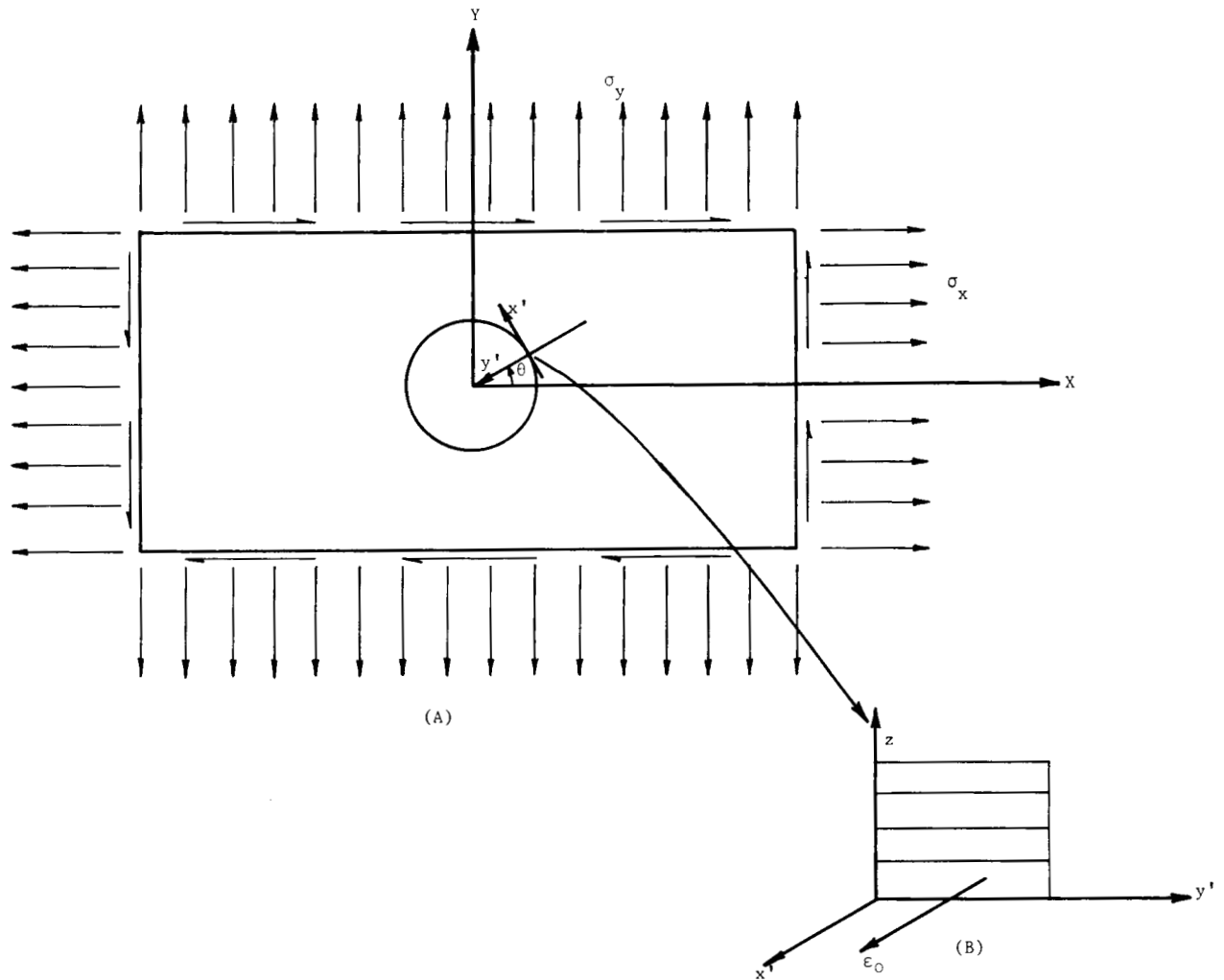


Figure 1

## PROCEDURE

The analysis procedure is summarized in the following figure. The combination of closed-form (CFH - closed-form, hole [1] and CHI - closed-form, inclusion [2]) and FEM [3] solutions provide efficiency and economy in the interpretation of results.

Note: CLT is a Classical Laminite Plate Theory Algorithm

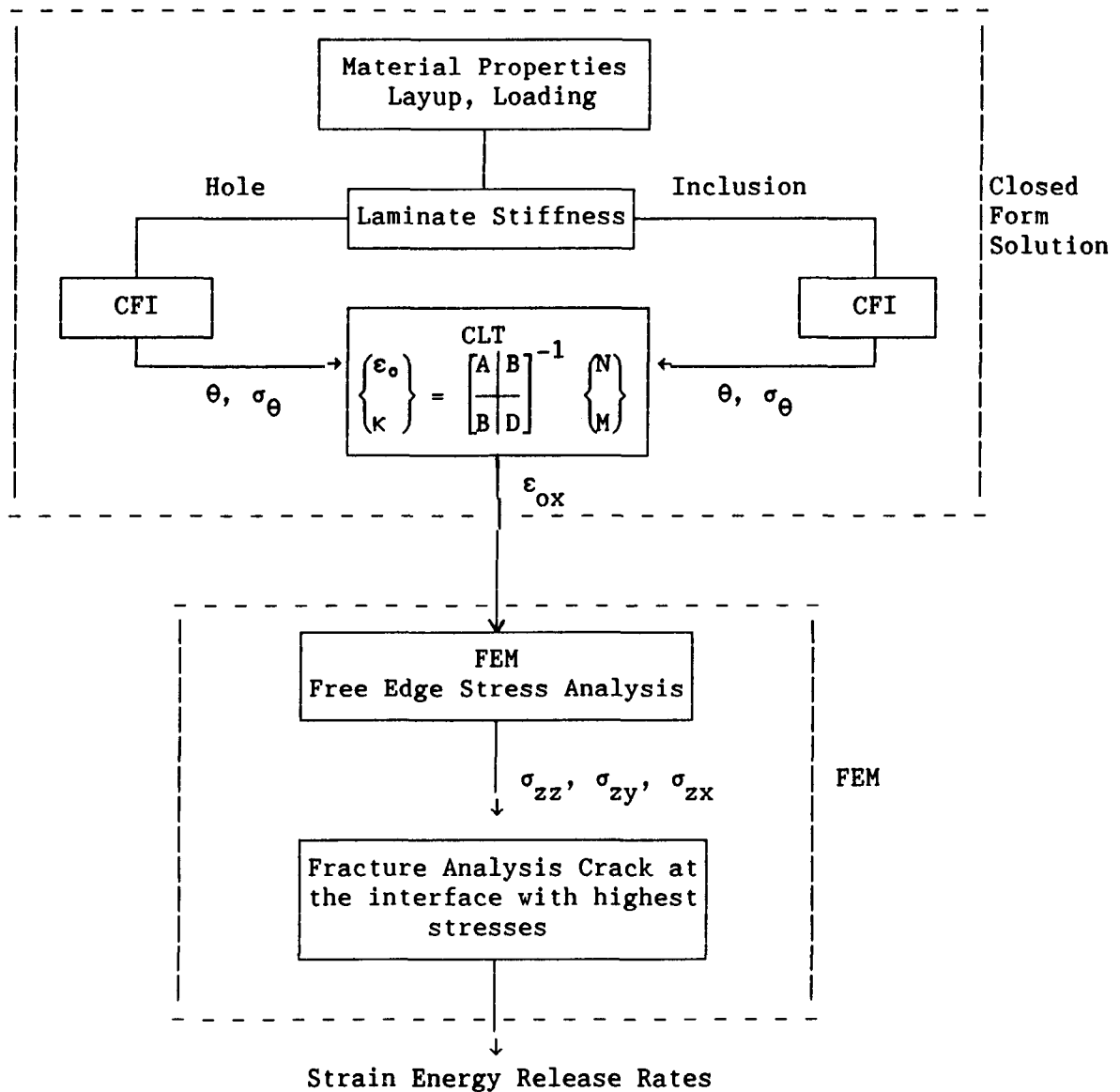


Figure 2.

# INPLANE STRAIN/STRESS RESULTS

{±35/0/90}<sub>s</sub> laminate is subjected to 5000 psi axial stress. The response of this laminate with a hole and with inclusions are tabulated below. The tangential stress is obtained from the closed-form solution and the strain is evaluated from CLT.

	E inclusion/ E plate	$\sigma_{\theta}/$ $\sigma_{\text{applied}}$	$\epsilon_o$
hole (w/o inclusion)	0	3.280	1710 $\mu\epsilon$
with soft inclusion (epoxy)	.169	1.865	972 $\mu\epsilon$
with rigid inclusion (steel)	3.128	.724	377 $\mu\epsilon$

Figure 3

## TANGENTIAL STRESS AROUND THE HOLE BOUNDARY

The tangential stress field for a laminate with a hole subjected to uniaxial tension and shear is presented in Figure 4. These stresses are displayed as a function of  $\theta$  around the boundary of the hole. As can be observed, the highest tangential stress is at  $\theta = 90^\circ$  for the tensile load and  $\theta = 50.5^\circ$  for the shear load.

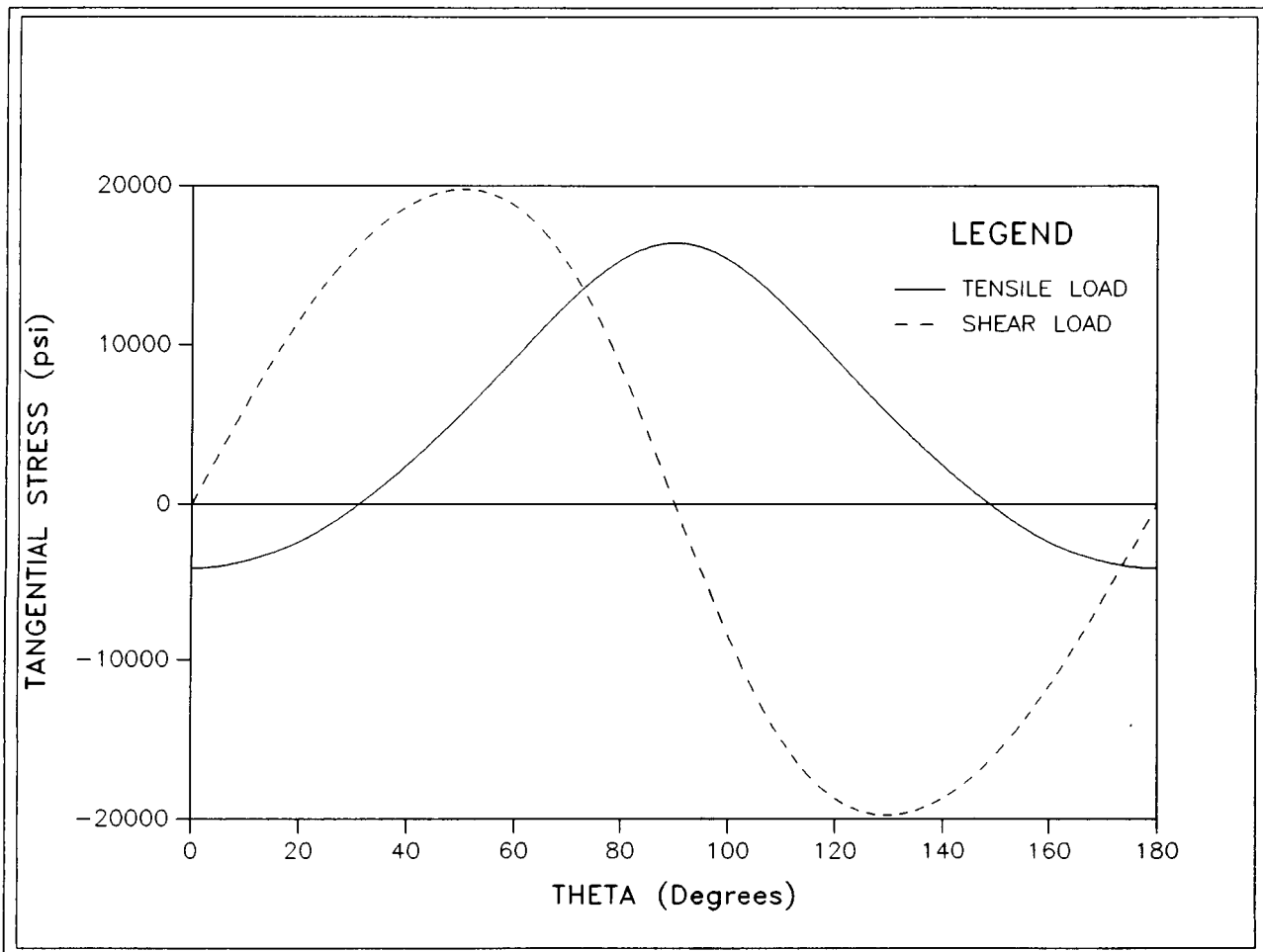


Figure 4

## INTERLAMINAR NORMAL STRESS VARIATION

The closed-form results of Figure 4 are converted to applied tensile strain,  $\epsilon_{ox} = 1710\mu\epsilon$  to be used in the FEM calculations. The FEM analysis models the laminate cross-section through-the-thickness and evaluates the interlaminar normal and shear stresses. Figure 5 presents the variation of the interlaminar normal stress along the y axis for each interface. Note that high stresses are at the free edge, between the 90/90 laminae and the 0/90 laminae.

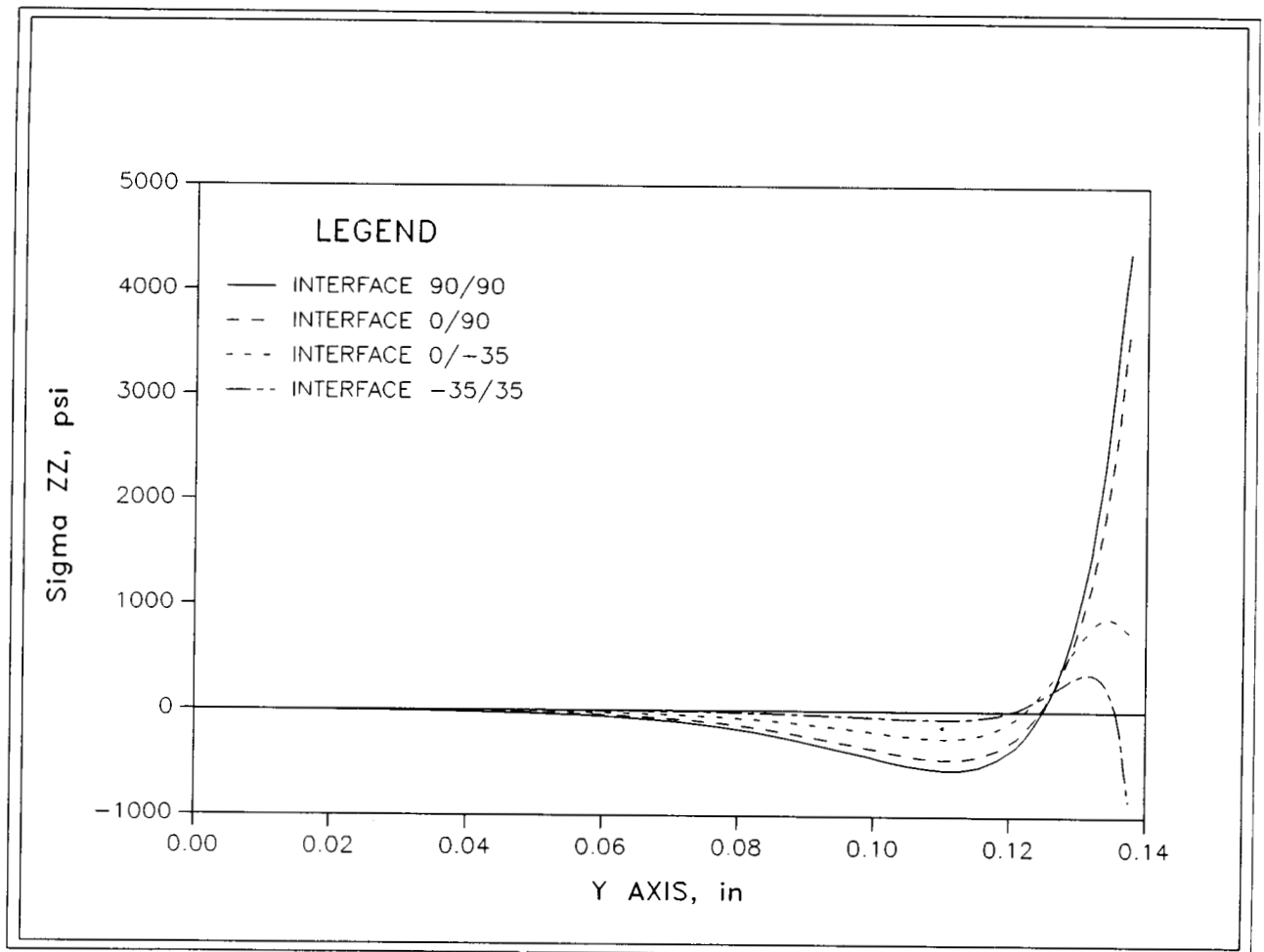


Figure 5

## INTERLAMINAR SHEAR STRESSES

Figure 6 presents the variation of the interlaminar shear stresses,  $\sigma_{zx}$  and  $\sigma_{zy}$ , along the Y-axis for each interface. It should be observed that the highest  $\sigma_{zx}$  is at the free edge between the -35/35 laminae and that  $\sigma_{zx}$  rapidly vanishes inside the laminate. Note that the highest  $\sigma_{zy}$  is just inside the laminate near the free edge between the 0/-35 laminae.

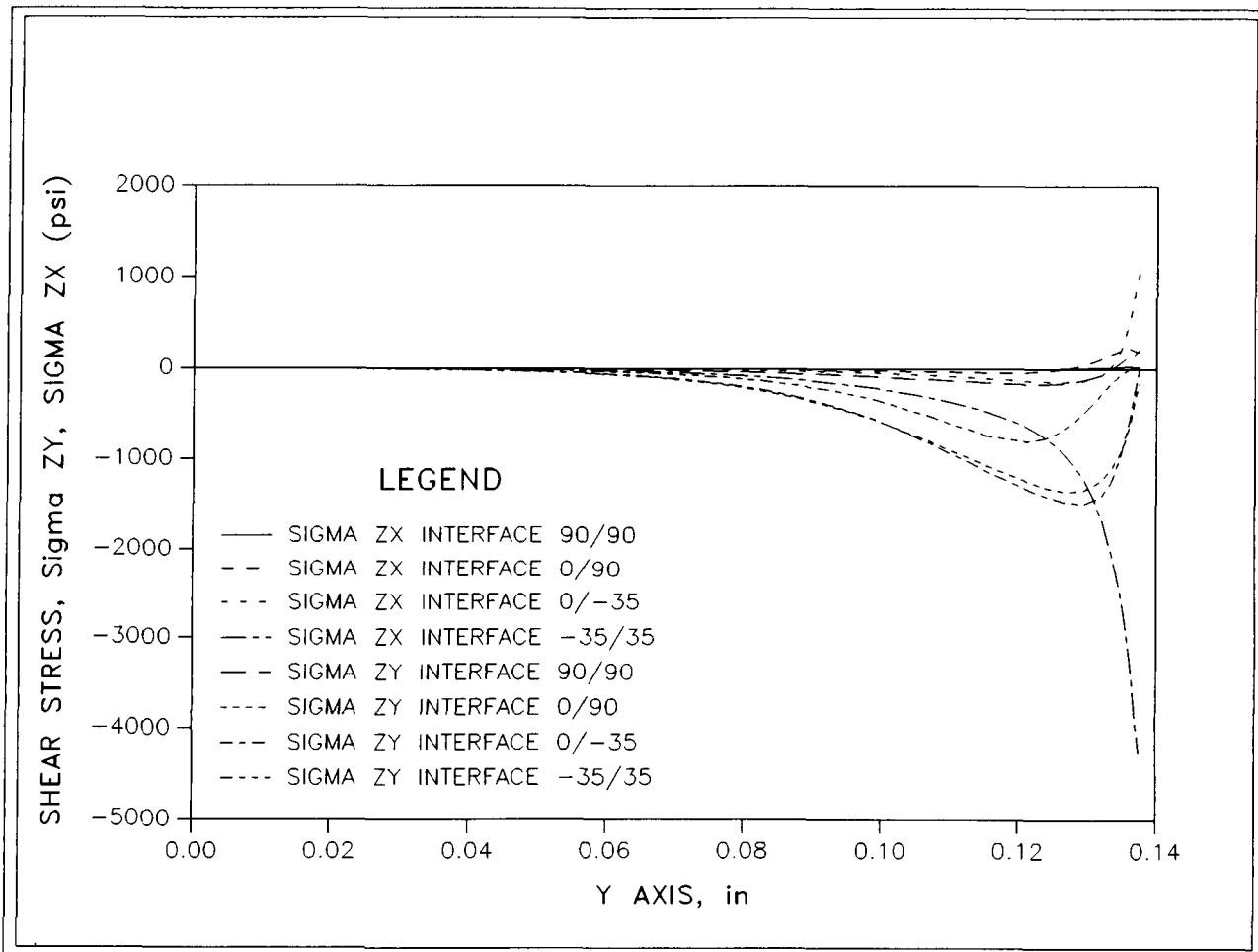


Figure 6

## INTERLAMINAR STRESSES THROUGH THE THICKNESS

Figure 7 presents a comparison of the relative magnitudes of  $\sigma_{zz}$ ,  $\sigma_{zx}$ ,  $\sigma_{zy}$  at the free edge through the thickness. As can be observed,  $\sigma_{zy}$  is much smaller than  $\sigma_{zz}$  and  $\sigma_{zx}$ .  $\sigma_{zz}$  is relatively large at the midplane, 90/90, and at the first interface, 0/90. The shear stress  $\sigma_{zx}$  is highest at the third interface, -35/35. The fourth interface is the top surface of the laminate and has no interlaminar stresses.

The strain energy release rates for this laminate are evaluated by modeling a crack of a length equal to the thickness of 8 plies at the 0/90 interface. The resulting ratios are  $G_I/G_{TOT} = .94096$  and  $G_{II}/G_{TOT} = .05827$ , indicating that Mode I behavior is dominant.

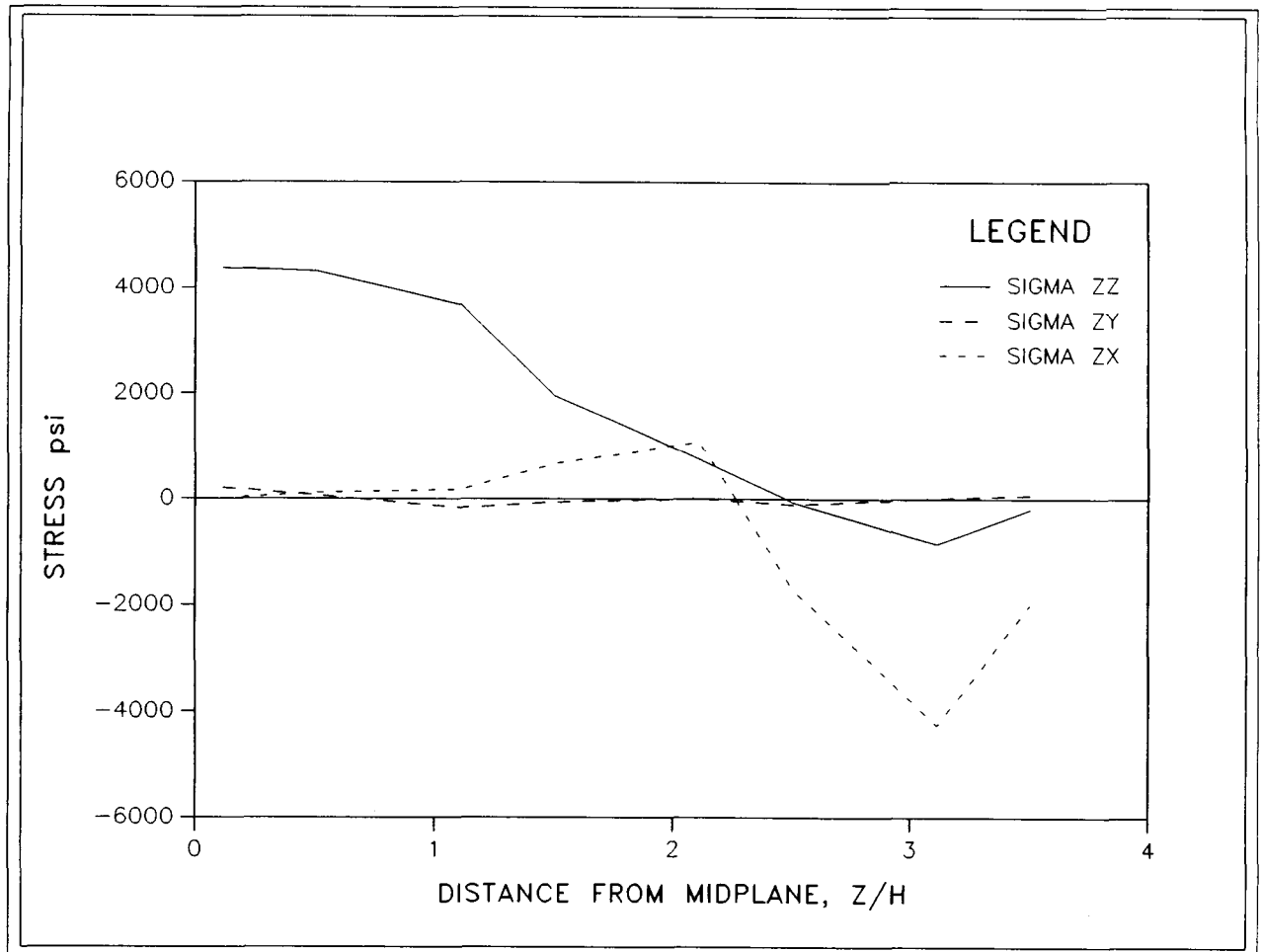


Figure 7



## DEFORMATION OF HOLE/INCLUSION BOUNDARY

The effects of inclusion moduli on deformation are displayed in Figure 8. As expected a soft inclusion results in larger displacements. The  $[\pm 35/0/90]_s$  laminate is loaded with uniaxial tensile stress of 50 ksi. The inclusion diameter is .5 inches.

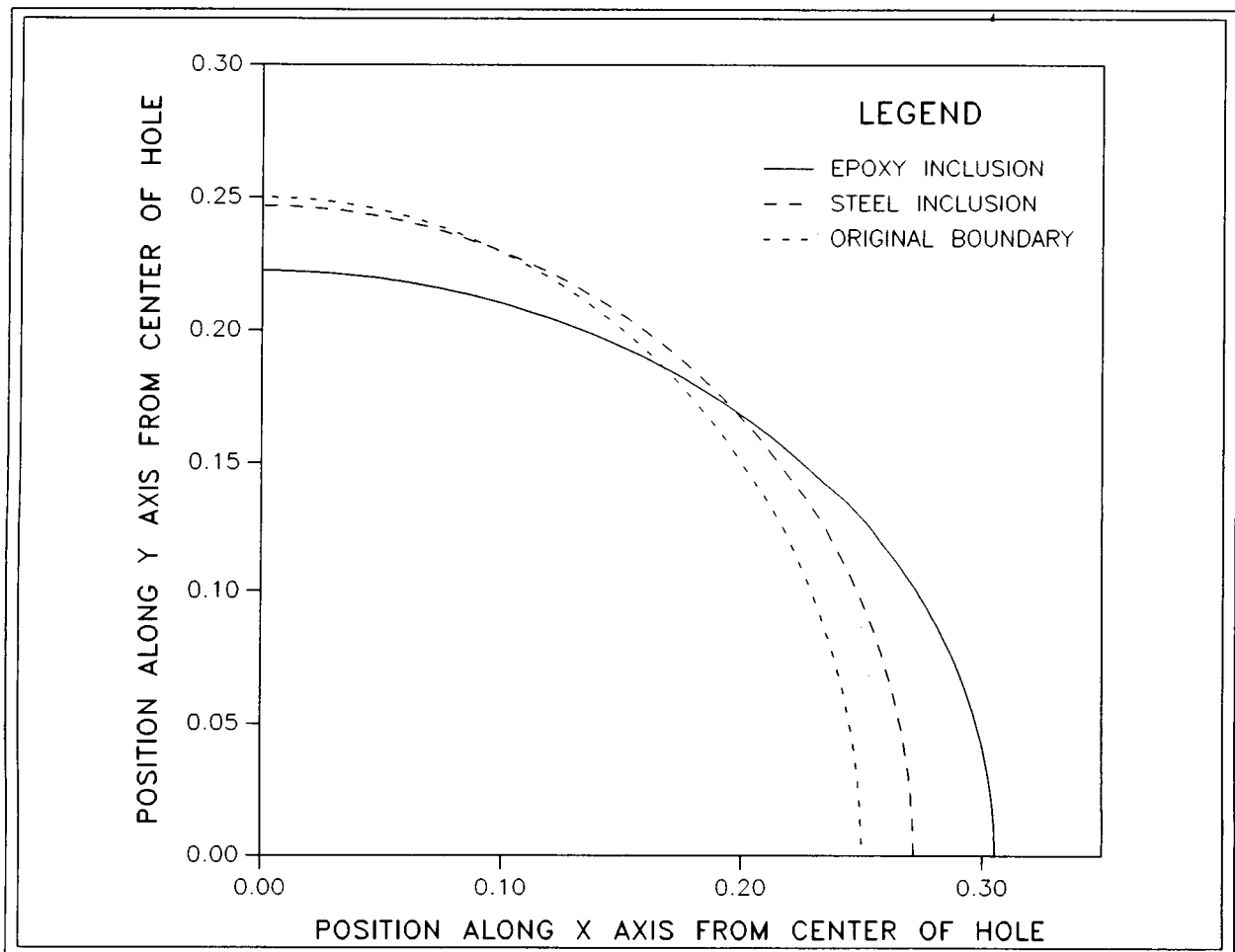


Figure 8

#### REFERENCES

1. S.C. Tan, "Composite Laminates Containing an Elliptical Opening," J. of Composite Materials.
2. S.G. Lekhnitskii, Anisotropic Plates, pp.190-218.
3. W.S. Chan and O.O. Ochoa, "Suppression of Edge Delamination In Composite Laminates By Terminating a Critical Ply Near the Edges," presented at the AIAA 29th SDM Conference, 1988.